

# Buckling









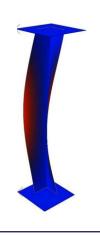


### Buckling

#### **Column buckling**

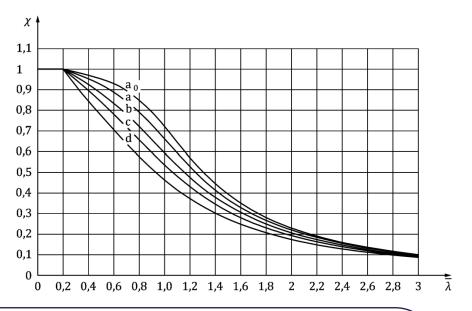
$$N_{cr} = \frac{\pi^2 EI}{L^2}$$

$$\uparrow$$
Euler's critical load



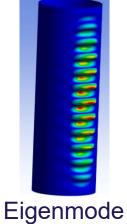
$$N_{b,Rd} = \frac{\chi N_{Rk}}{\gamma_{M1}}$$

$$\bar{\lambda} = \sqrt{\frac{N_{Rk}}{N_{cr}}}$$



#### Shell buckling (bending)

$$M_{cr} = \frac{\pi C_m}{\sqrt{3(1-\nu)^2}} Ert^2$$



$$M_{b,Rd} = \frac{\chi M_{pl,I}}{\gamma_{M1}}$$

$$\bar{\lambda} = \sqrt{\frac{M_{pl,I}}{M_{cr}}}$$

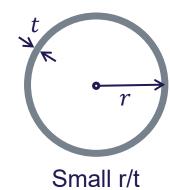


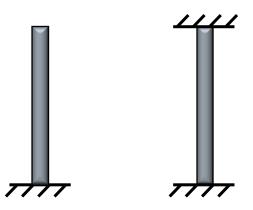


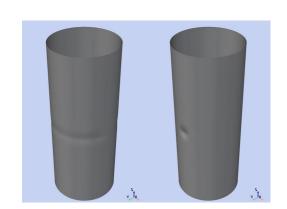
Results

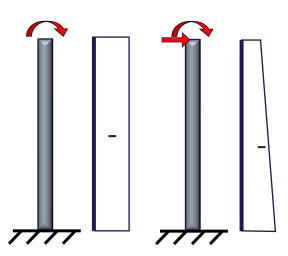
### **Differences**

	Assumptions in EN 1993-1-6	Conditions in monopile
Static system	Supported at both ends	Cantilever
r/t ratio	Range of validity: 50 – 2000	35 – 65
Imperfection form	Full-circumferential dimple	Dimple of limited size
Moment distribution	Uniform moment	Increasing moment









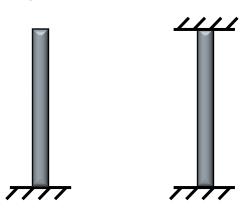


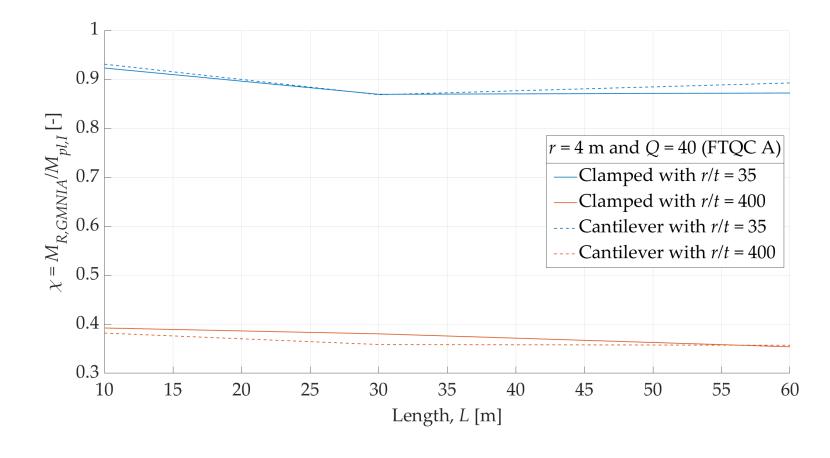
Static system r/t ratio Imperfection form Moment distribution

### Static system

#### Based on a brief study

- Limited effect
- Small relative difference-2.7% and 2.3%
- No obvious correlation with geometric parameters







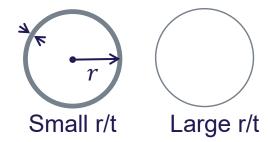
Static system

r/t ratio

Imperfection form

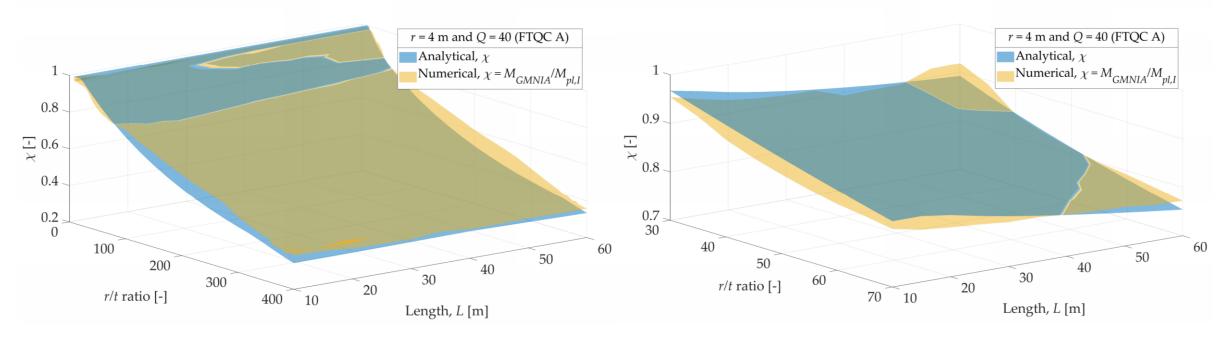
**Moment distribution** 

### r/t ratio



#### All investigated geometries





Mostly unconservative analytical results for r/t < 50 and for typical monopile geometries.



Static system

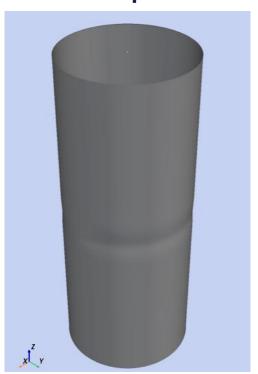
r/t ratio

Imperfection form

**Moment distribution** 

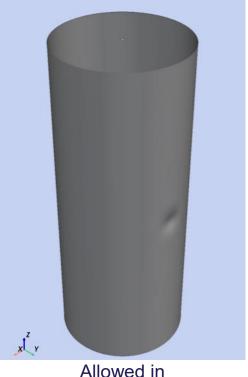
### Imperfection form

## Full-circumferential dimple



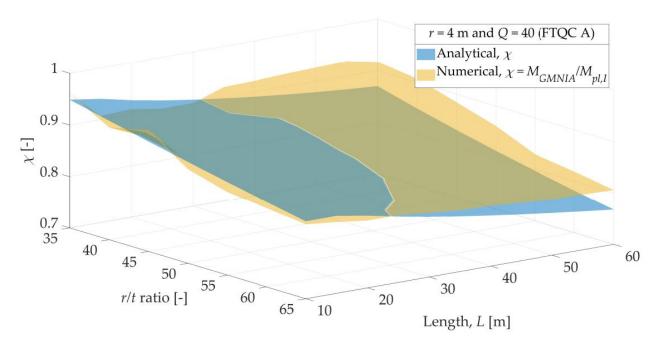
Assumed in analytical methods

**Limited dimple** 



Allowed in execution standard

# Limited dimple vs. analytical method (with full-circumferential dimple)

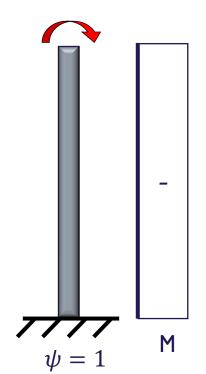


Still some unconservative analytical results for typical monopile geometries.

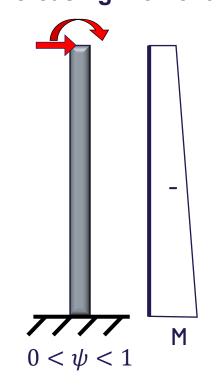


### Moment distribution

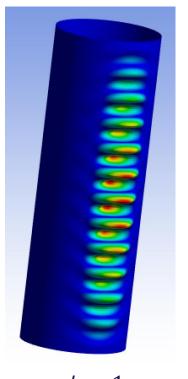
#### **Uniform moment**



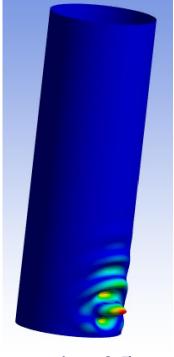
#### **Increasing moment**



#### **Buckling modes**







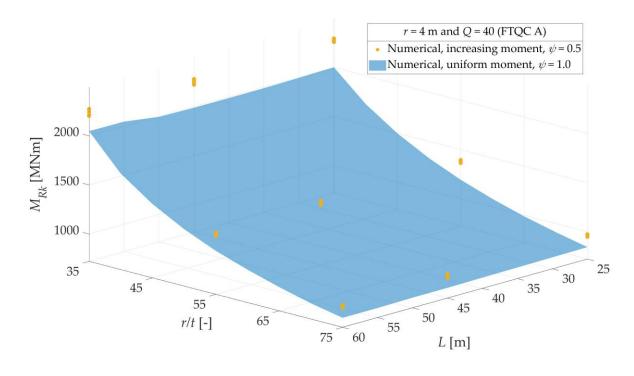
$$\psi = 0.5$$



Introduction Differences Results
Static system r/t ratio Imperfection form Moment distribution

# **Moment** distribution

● Uniform moment → linearly increasing moment → min. 7% increase in resistance





### Thank you for your attention!



